ON SCIENTIFIC CONTACTS
WITH SERGEI ALEKSANDROVICH TELYAKOVSKII

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The paper presents some memories of the joint research with the prominent specialist in the theory of functions of a real variable Sergei Aleksandrovich Telyakovskii.

Keywords: S.A. Telyakovskii.

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