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## ON THE REDUCTION OF SYSTEMS WITH INCOMMENSURATE DELAYS TO A FORM WITH ZERO DYNAMICS

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A form with zero dynamics for time-delay systems is considered. The results obtained earlier for the case of commensurate delays are transferred to systems with incommensurate delays. Conditions are obtained under which the reduction to such a form is possible, and an algorithm for constructing the corresponding transformation is described.

Keywords: time-delay systems, incommensurate delays, zero dynamics.

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