

**MORITA EQUIVALENCE CLASSES OF PRINCIPAL BLOCKS
WITH ELEMENTARY ABELIAN DEFECT GROUPS OF ORDER 64¹**

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MSC: Primary 20C20; Secondary 16D90, 20C05

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We classify the Morita equivalence classes of principal blocks with elementary abelian defect groups of order 64 with respect to a complete discrete valuation ring with an algebraically closed residue field of characteristic two.

Keywords: Donovan's conjecture, finite groups, Morita equivalence, block theory, modular representation theory.

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