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ANALYSIS OF A THEOREM ON THE JACKSON–STECHKIN INEQUALITY IN THE BERGMAN SPACE B_2

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We present a refinement of a theorem of V. A. Abilov, F. V. Abilova, and M. K. Kerimov on the exact constant in a Jackson type inequality between the mean-square approximation of a function of a complex variable by Fourier series in a system orthogonal in a bounded domain and the generalized modulus of continuity of order $m \geq 1$.

Keywords: generalized modulus of continuity, generalized translation operator, orthonormal system, Jackson–Stechkin inequality.

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