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CODES IN DISTANCE-REGULAR GRAPHS WITH  $\theta_2 = -1$ 

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If a distance-regular graph  $\Gamma$  of diameter 3 contains a maximal 1-code  $C$  that is both locally regular and last subconstituent perfect, then  $\Gamma$  has intersection array  $\{a(p+1), cp, a+1; 1, c, ap\}$  or  $\{a(p+1), (a+1)p, c; 1, c, ap\}$ , where  $a = a_3$ ,  $c = c_2$ , and  $p = p_{33}^3$  (Jurišić and Vidali). In first case,  $\Gamma$  has eigenvalue  $\theta_2 = -1$  and the graph  $\Gamma_3$  is pseudogeometric for  $GQ(p+1, a)$ . In the second case,  $\Gamma$  is a Shilla graph. We study graphs with intersection array  $\{a(p+1), cp, a+1; 1, c, ap\}$  in which any two vertices at distance 3 are in a maximal 1-code. In particular, we find four new infinite families of intersection arrays:  $\{a(a-2), (a-1)(a-3), a+1; 1, a-1, a(a-3)\}$  for  $a \geq 5$ ,  $\{a(2a+3), 2(a-1)(a+1), a+1; 1, a-1, 2a(a+1)\}$  for  $a$  not congruent to 1 modulo 3,  $\{a(2a-3), 2(a-1)(a-2), a+1; 1, a-1, 2a(a-2)\}$  for even  $a$  not congruent to 1 modulo 3, and  $\{a(3a-4), (a-1)(3a-5), a+1; 1, a-1, a(3a-5)\}$  for even  $a$  congruent to 0 or 2 modulo 5.

Keywords: distance-regular graph, maximal code.

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