Vol. 21 No. 3

2015

ON INTERSECTIONS OF ABELIAN AND NILPOTENT SUBGROUPS IN FINITE GROUPS

V.I.Zenkov

Received June 21, 2015

Let A be an abelian subgroup of a finite group G, and let B be a nilpotent subgroup of G. If G is solvable, then we prove that it contains an element g such that $A \cap B^g \leq F(G)$, where F(G) is the Fitting subgroup of G. If G is not solvable, we prove that a counterexample of smallest order to the conjecture that $A \cap B^g \leq F(G)$ for some element g of G is an almost simple group.

Keywords: finite group, abelian subgroup, nilpotent subgroup, intersection of subgroups, Fitting subgroup.

V. I. Zenkov Dr. Phys.-Math. Sci., Prof., Krasovskii Institute of Mathematics and Mechanics, Ural Branch of the Russian Academy of Sciences, Yekaterinburg, 620990 Russia; Ural Federal University, Yekaterinburg, 620002 Russia, e-mail: v1i9z52@mail.ru.

Cite this article as:

V. I. Zenkov, On intersections of abelian and nilpotent subgroups in finite groups, *Tr. Inst. Mat. Mekh. UrO RAN*, 2015, vol. 21, no. 3, pp. 128–131.