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ON THE CONTINUOUS EXTENSION OF A GENERALIZED SOLUTION OF THE HAMILTON–JACOBI EQUATION BY CHARACTERISTICS THAT FORM A CENTRAL FIELD OF EXTREMALS

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The Cauchy problem for the Hamilton–Jacobi equation with state constraints is considered. A justification for a construction of a generalized solution with given structure is provided. The construction is based on the method of characteristics and on solutions of problems related to calculus of variations.

Keywords: Hamilton–Jacobi equations, method of characteristics, viscosity solutions, minimax solutions, calculus of variations, extremals.

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